

# 1 **Supporting Information**

## 2 **Appendix S1** Description of the water budget model.

3 The monthly potential evapotranspiration ( $PET_m$ ) was computed using the Turc equation  
4 (Turc, 1961) (see eqn S1).

$$5 \quad PET_m = n \times 0.0133333 \times (Rg_m + 50) \times (t_m / (t_m + 15)) \quad \text{eqn S1}$$

6 with  $n$  = number of days of the month,  $t_m$  = the monthly temperature and  $Rg_m$  = the monthly  
7 potential radiation.

8 The water budget computed monthly soil water content ( $SWC_m$ ) for each plot over the  
9 period 1980-2001, with initial condition for January 1980  $SWC_m$  set as  $SWC_{max}$  (the  
10 maximum soil water content). Then monthly soil water content was iteratively computed  
11 using eqn S2.

$$12 \quad SWC_{m+1} = \min(SWC_m + Precip_{s\ m} - AET_m, SWC_{max}) \quad \text{eqn S2}$$

13 With  $Precip_{s\ m}$  = the infiltrating precipitation,  $AET_m$  = the monthly actual evapotranspiration  
14 computed by eqn S3.

$$15 \quad AET_m = \min(D_m, S_m) \quad \text{eqn S3}$$

16 with  $D_m = PET_m - Precip_{i\ m}$  where  $Precip_{i\ m}$  is the the intercepted precipitation.

17 and  $S_m = c_w * SWC_m / SWC_{max}$  where  $c_w$  is a parameter denoting the maximum

18 evapotranspiration from a saturated soil under conditions of high demand (as in Bugmann &  
19 Cramer 1998 we assume that  $c_w = 12$  cm/month).

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21  $Precip_{i\ m}$  and  $Precip_{s\ m}$  are computed with eqns S4 and S5

$$22 \quad Precip_{i\ m} = \min(f_i * P_m, PET_m) \quad \text{eqn S4}$$

23 with  $f_i$  = a parameter denoting the fraction of precipitation that is intercepted and is set at a  
24 value of 0.3 following Bugmann & Cramer (1998), and  $P_m$  = the monthly precipitation.

$$25 \quad Precip_{s\ m} = P_m - Precip_{i\ m} \quad \text{eqn S5}$$

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## 27 **References**

28 Bugmann, H. & Cramer, W. (1998) Improving the behaviour of forest gap models along  
29 drought gradients. *Forest Ecology and Management*, **103**, 247-263.

30 Turc, L. (1961) Evaluation des besoins en eau d'irrigation, évapotranspiration potentielle.

31 *Annales Agronomiques*, **12**, 13-49.

## 32 **Appendix S2** Likelihood of the model and prior description.

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34 The likelihood of the observed five years radial growth ( $y_{pi}$ ) based on a log-normal  
35 distribution of mean  $G_{pi}$  (see eqn 1) and variance  $\sigma^2$  is given by eqn S6.

$$36 \quad L(Y | X, \sigma^2) = \prod_{p=1}^P \prod_{i=1}^{N_p} \text{LN}(y_{pi} | G_{pi}, \sigma^2) \quad \text{eqn S6}$$

37 We used flat conjugate prior with inverse-gamma distribution for variance  $\sigma^2$  and conjugate  
38 log-normal prior for  $\alpha_p, \beta_1, \beta_2,$  and  $\beta_3$  and non informative unconjugate prior for  $\gamma$  and  $\delta$ . The  
39 first level priors were log-normal prior for  $\beta$   $p(\log(\beta_k)) = N(\text{mean}=0, \text{precision}=0.000001)$ ,  
40 inverse-gamma for  $\sigma^2$   $p(\sigma^2) = IG(1,0.1)$ , a uniform prior for  $\gamma$ , a normal prior for  $\delta$   
41  $p(\delta) = N(\text{mean} = 0, \text{precision} = 0.000001)$ .  $\alpha_p$  was modelled as a random log-normal variable  
42 accounting for plot effect, with mean  $\alpha$  and variance  $V_p$  ( $p(\alpha_p) = \text{LN}(\alpha, V_p)$ ). The second  
43 level priors were a flat inverse-gamma prior  $p(V_p) = IG(1,0.1)$  and non informative log-  
44 normal prior  $p(\log(\alpha)) = N(\text{mean} = 0, \text{precision} = 0.000001)$ .

45 To keep the parameters within a biologically meaningful range and to help MCMC  
46 convergence we bounded prior within a plausible range of values. Studies have generally  
47 concluded that there is a positive effect of degree-day sum ( $DD$ ), and a negative effect of  
48 drought, on tree growth (see Rickebusch *et al.* 2007). We therefore decided to constrain our  
49 estimation to have a positive effect of both  $DD$  and  $WB$  by setting a positive boundary to the  
50 prior.

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## 52 **References**

53 Rickebusch, S., Lischke, H., Bugmann, H., Guisan, A. & Zimmermann, N.E. (2007)  
54 Understanding the low-temperature limitations to forest growth through calibration of forest  
55 dynamics models with tree-ring data. *Forest Ecology and Management*, **246**, 251-263.

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57 **Table S1:** Year of data collection and area for each *Département*.

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<b>Département</b>	<b>Year of data collection</b>	<b>Area (km<sup>2</sup>)</b>
1	1995	5762
4	1999	6925
5	1997	5549
6	2002	4299
25	1994	5234
26	1996	6530
38	1997	7431
39	1992	4999
73	2000	6028
74	1998	4388
83	1999	5973
84	2001	3567

65 **Table S2.** Parameter estimates of the growth model (see eqn 1 for details): mean posterior values (and 95% posterior credible intervals) for the fixed-  
66 effects of the best model (see Table 2). ‡ indicates that the parameter was not estimated for this species. For species acronyms, see Table 1.

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Species	$\alpha$	$\beta_1$	$\beta_2$	$\beta_3$	$\gamma$	$\delta$	$\delta_1$	$\delta_2$
<b>ABIALB</b>	2.56 (2.01 - 3.47)	0.42 (0.41 - 0.44)	0.15 (0.11 - 0.19)	0.14 (0.11 - 0.17)	0.17 (0.09 - 0.25)	1.05 (0.86 - 1.27)	0.1 (0.02 - 0.19)	‡
<b>FAGSIL</b>	0.96 (0.87 - 1.09)	0.43 (0.42 - 0.44)	0.07 (0.03 - 0.1)	0.08 (0.06 - 0.1)	0.34 (0.26 - 0.4)	1.04 (0.87 - 1.23)	-0.29 (-0.38 - -0.2)	0.15 (0.06 - 0.26)
<b>PICABI</b>	3.08 (2.5 - 3.95)	0.44 (0.43 - 0.45)	0.3 (0.24 - 0.35)	0.13 (0.1 - 0.16)	0.09 (0.05 - 0.14)	0.91 (0.8 - 1.02)	0.16 (0.11 - 0.21)	0 (-0.03 - 0.04)
<b>PINSYL</b>	1.07 (0.94 - 1.24)	0.1 (0.09 - 0.11)	0 (0 - 0.01)	0.01 (0 - 0.03)	0.18 (0.12 - 0.25)	0.85 (0.72 - 0.99)	‡	‡
<b>LARDEC</b>	1.67 (1.14 - 2.6)	0.26 (0.24 - 0.27)	0.15 (0.08 - 0.25)	0.06 (0.03 - 0.09)	0.1 (0.02 - 0.25)	0.6 (0.45 - 0.8)	0.12 (0.04 - 0.23)	‡
<b>QUEPET</b>	1.62 (1.16 - 2.22)	0.44 (0.42 - 0.46)	0.12 (0.09 - 0.15)	0.07 (0.03 - 0.12)	0.05 (0.02 - 0.13)	0.59 (0.48 - 0.73)	‡	-0.02 (-0.07 - 0.02)
<b>QUEPUB</b>	0.5 (0.46 - 0.54)	0.19 (0.18 - 0.2)	0.1 (0.08 - 0.11)	0.04 (0.02 - 0.07)	0.34 (0.27 - 0.42)	0.72 (0.6 - 0.86)	‡	0.2 (0.1 - 0.31)
<b>QUEROB</b>	1.86 (1.22 - 3.43)	0.33 (0.29 - 0.36)	0.17 (0.09 - 0.26)	0.03 (0 - 0.07)	0.13 (0.01 - 0.34)	0.59 (0.42 - 0.82)	0.02 (-0.09 - 0.14)	‡
<b>QUEILE</b>	0.46 (0.42 - 0.51)	0.15 (0.14 - 0.16)	0.14 (0.11 - 0.17)	0.09 (0.06 - 0.11)	0.18 (0.03 - 0.46)	0.13 (0.06 - 0.19)	‡	‡
<b>PINCEM</b>	1.4 (0.64 - 3.19)	0.01 (-0.08 - 0.09)	0.04 (0 - 0.11)	0.13 (0.02 - 0.26)	0.17 (0.01 - 0.58)	0.8 (0.46 - 1.3)	‡	‡
<b>PINUNC</b>	0.86 (0.58 - 1.45)	0.1 (0.07 - 0.14)	0.03 (0 - 0.08)	0.09 (0.04 - 0.15)	0.22 (0.05 - 0.43)	1 (0.66 - 1.46)	‡	‡
<b>POPTRE</b>	1.84 (1.24 - 3.38)	0.28 (0.24 - 0.32)	0.09 (0.03 - 0.15)	0.08 (0.02 - 0.13)	0.17 (0.02 - 0.35)	0.81 (0.54 - 1.13)	‡	‡
<b>ACEg</b>	1.56 (1.09 - 2.37)	0.26 (0.23 - 0.29)	0.05 (0.01 - 0.11)	0.12 (0.08 - 0.16)	0.19 (0.05 - 0.38)	0.85 (0.61 - 1.18)	0.03 (-0.1 - 0.17)	
<b>BETPUB</b>	1.65 (1.11 - 2.64)	0.1 (0.05 - 0.15)	0.03 (0 - 0.08)	0.1 (0.02 - 0.19)	0.15 (0.03 - 0.33)	0.77 (0.54 - 1.04)	‡	0.08 (-0.07 - 0.27)
<b>CARBET</b>	1.16 (0.87 - 1.68)	0.3 (0.29 - 0.31)	0.1 (0.07 - 0.13)	0.08 (0.04 - 0.13)	0.15 (0.05 - 0.26)	0.9 (0.69 - 1.13)	‡	-0.01 (-0.12 - 0.07)
<b>FRA</b>	1.66 (1.23 - 2.41)	0.36 (0.34 - 0.38)	0.07 (0.04 - 0.1)	0.11 (0.08 - 0.15)	0.14 (0.04 - 0.25)	0.77 (0.57 - 1)	‡	‡

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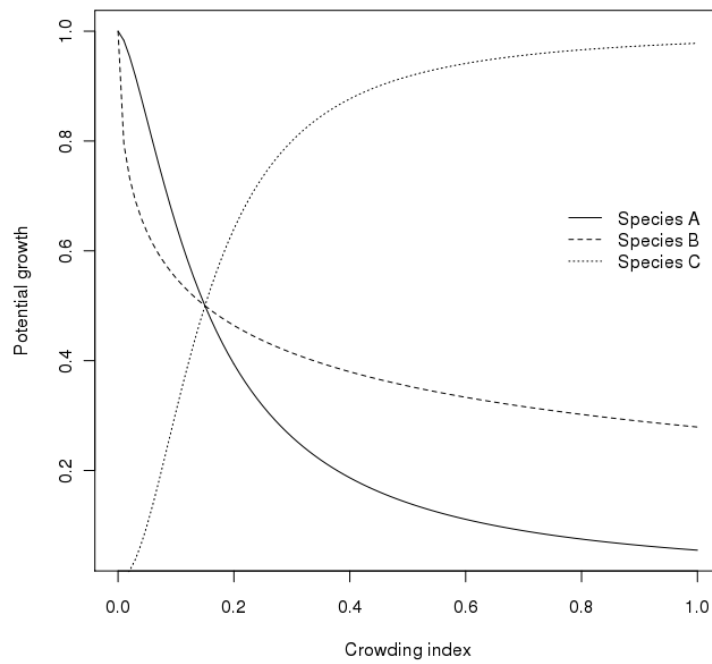
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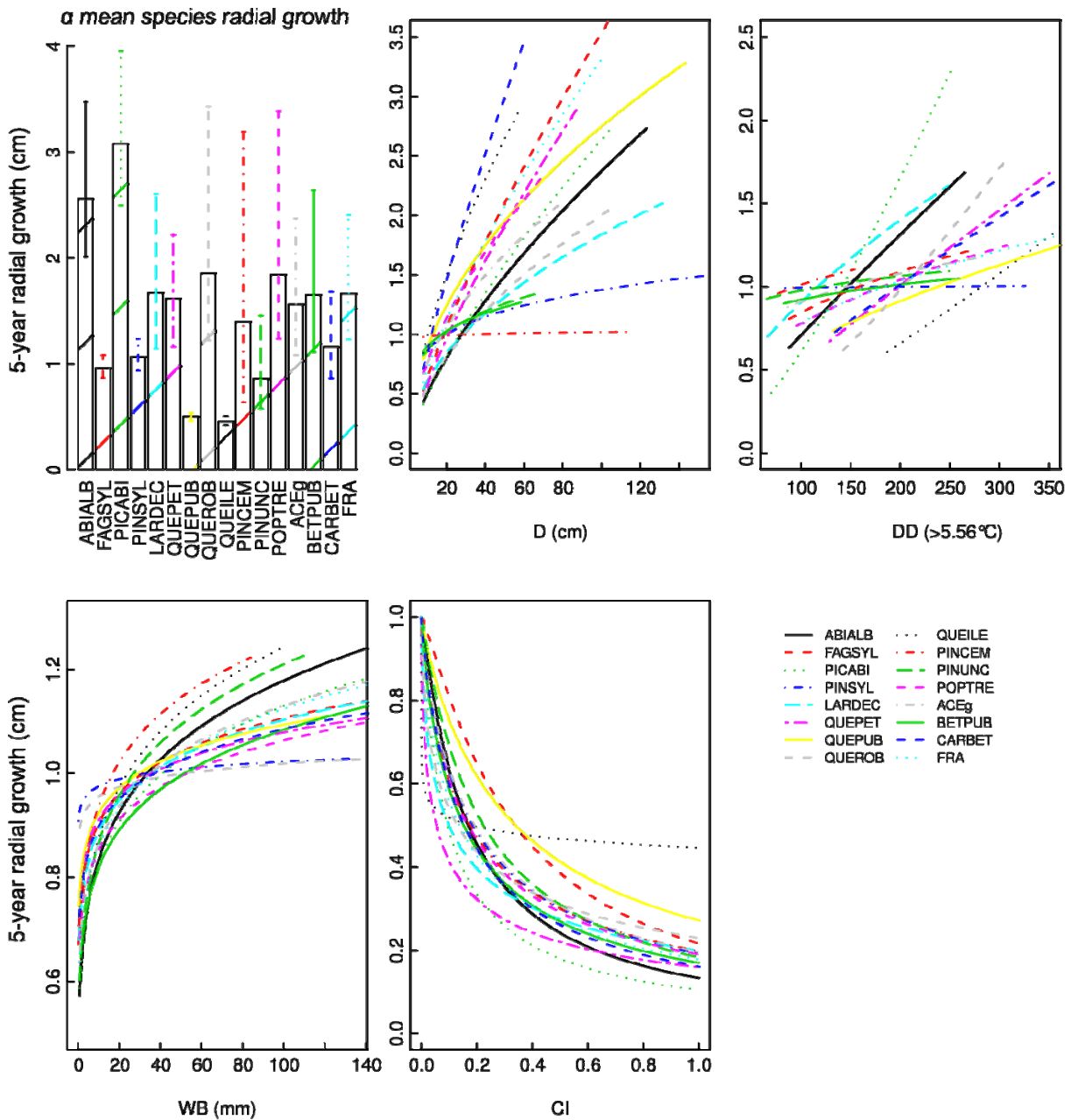
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75 **Fig. S1.** Effect of neighbourhood crowding on potential growth for three hypothetical species.  
76 Species A exhibits a very strong decrease of potential growth at high crowding index ( $\delta=1.5$   
77 and  $\gamma=0.15$ ), whereas Species B exhibits a much smaller reduction of potential growth ( $\delta=0.5$   
78 and  $\gamma=0.15$ ). Finally, Species C exhibits a positive crowding effect (i.e. facilitation) ( $\delta=-2$  and  
79  $\gamma=0.15$ ). The crowding reduction function and crowding index range between 0 and 1. See  
80 text for more details on the crowding function.



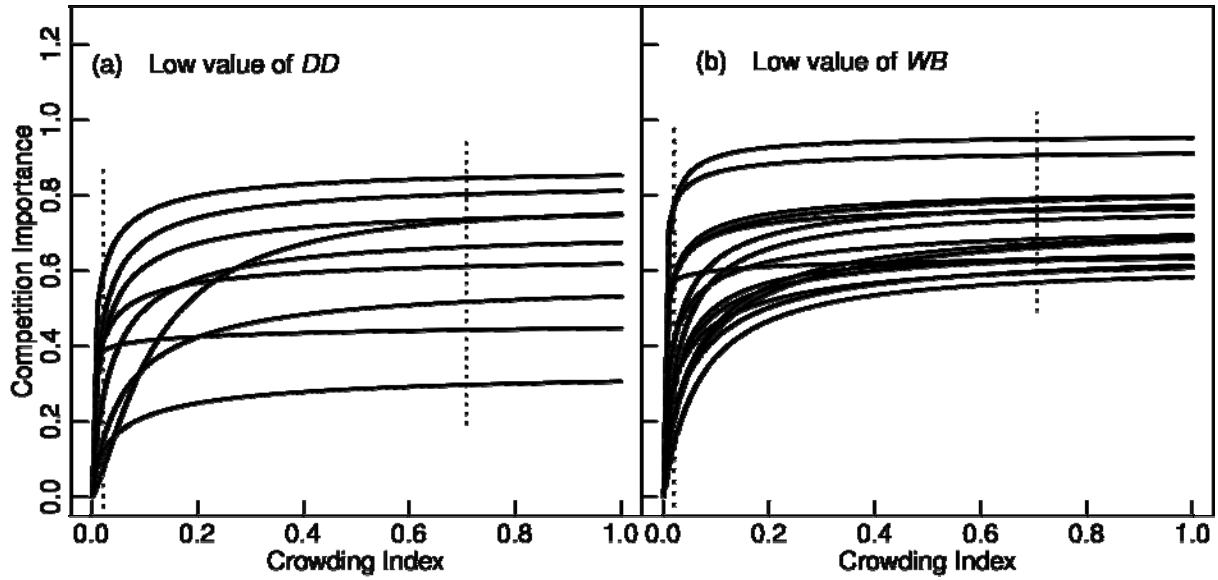
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**Fig S2.** Growth response curves. For each of the 16 studies species, growth parameters  $\alpha$  (and 95% credible intervals) (a), and growth curves showing the effect of (b) diameter ( $D$ ), (c) degree-day sum ( $DD$ ), (d) water budget ( $WB$ ) and (e) crowding index ( $CI$ ), for the 16 studied species. See Table 1 for species acronyms.



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102 **Fig. S3.** Variation in competition importance with crowding index at low values of degree-  
103 day sum ( $DD$ ) (high stress) (a) and low value of water budget ( $WB$ ) (high stress) (b). Vertical  
104 dotted lines represents positions of low and high crowding conditions ( $CI$  of 0.02 and 0.7  
105 respectively) used in Figs. 6 and 7 in the main text.



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